Correlational Studies of	GUINNESS DRAUGHT	
Differences between Means		



Correlation: relation between variables

Focus on relations between two score variables Prediction: predict the value of one variable (predicted variable) from the value of another variable (predictor variable)

Predict how far a value on one variable differs from the mean of that variable based on how far the value on the other variable differs from its mean

Pearson coefficient

Prediction based on regression line

Regression coefficient
 Regression constant

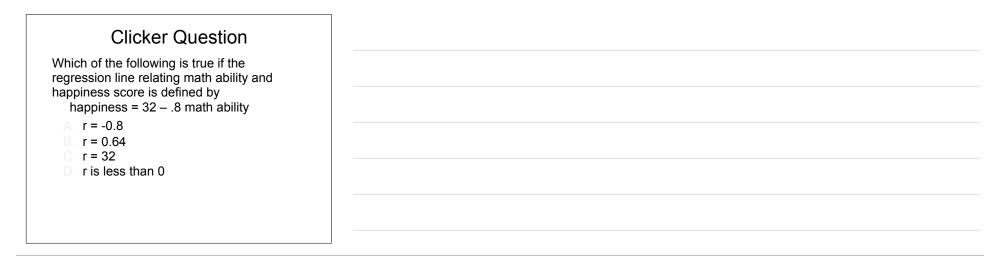


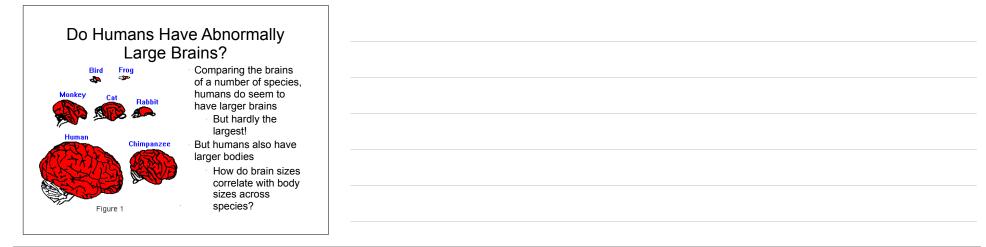


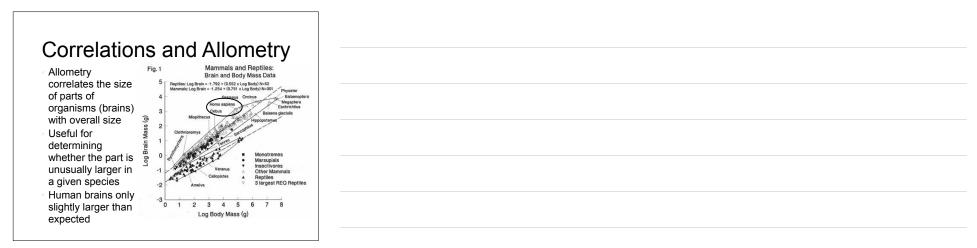
### **Clicker Question**

For the correlation between the average speed a person drives and gas mileage, r = -.80. The correlation accounts for

- A -80% of the variance
- A. -80% of the variance
- 80% of the variance
- 64% of the variance
- D. Cannot tell from the information given







Correlations in samples and	
populations	
The interest in correlations typically goes beyond	
the sample studied—investigators want to know	
about the broader population.	
Two approaches	
<ul> <li>Estimating correlation in population (ρ) from correlation in sample (r)</li> </ul>	
Confidence interval	
- Determining whether there is a correlation in a	
given direction in the real population from	
correlation in sample	
Statistical significance	
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Statistical significance and p-values	
Fundamental question: How likely is it that the result (correlation in the sample) is due to chance rather than a	
real correlation in the population?	
<ul> <li>Formally: How statistically significant is the correlation?</li> <li>How likely is a given correlation in the sample if there</li> </ul>	
were <b>no correlation</b> (or a correlation in the other	
direction) in the population?	
<ul> <li>This is specified by the p-value</li> <li>A p-value &lt; .05 means there is less than a 1 chance in</li> </ul>	
20 of a correlation in the sample without a correlation	
in the real population That is, more than 19 times out of 20 the correlation	

found in the sample is due to a correlation in the real population`

#### Statistical significance and p-values

p-values typically reported as less than some value

- <.05 is the most commonly used significance level If a study reports that the results are statistically significant with no p value, usually p<.05 is the intended meaning
- <.01 is a higher, more demanding significance level Less than 1 chance in 100 of getting the result by chance

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- For some purposes, lower p values are useful to know
- Prediction with reliably of only .10 or .25 could be important to know

Chemical exposure and cancer, etc.

Clicker Question
A study reports a negative correlation between cell phone use and age at death with $p<.15$ . From this you should conclude
<ul> <li>A. There is no correlation between cell phone use and age at death since p is not less than .05</li> <li>B. There is less than a 15% chance that the</li> </ul>
correlation is due to chance ⊂. There is less than a 15% chance of a correlation in the actual population
D. There is at least a 15% chance that the correlation is due to chance

## Significance vs. Importance

- A statistically significant finding may or may not be important.
  - All statistical significance means is that the finding is statistically reliable—not likely to have occurred by chance
  - where the p-value specifies what we count as likely
- Whether it is important—worth knowing depends on the finding

#### Correlations are hard to detect

- Humans are terrible at recognizing intuitively whether two variables are correlated
  - We see correlations where none exist
    We fail to see correlations that do exist
- Must actually look at the evidence, not rely on our impressions
  - Perform statistical analyses!

<ul> <li>Fallacies of Prediction</li> <li>Seeing correlations that don't exist</li> <li>Failing to recognize regression to the mean</li> <li>Explaining streaks that are to be expected</li> <li>Failing to consider base rates</li> </ul>	
Fallacy of Prediction 1: Seeing	
<ul> <li>correlations that don't exist</li> <li>"When I'm waiting for the bus, the one going in the other direction always comes first!"</li> <li>Evelyn Marie Adams won the New Jersey lottery twice, a 1 in 17 trillion likelihood—seem unlikely?</li> <li>Given the millions of people who buy</li> </ul>	
state lottery tickets, it was practically a sure thing that someone, someday, somewhere would win twice.	

# Coincidences happen

- Adams, Jefferson, and Monroe, three of the first five presidents of the US, died on the same date—July 4!
- Charles Schulz died of a heart attack on the day his last published Peanuts cartoon!

Fallacy of Prediction 2: Failing to	
Tallacy of Theulolion 2. Talling to	
recognize regression to the mean	
<b>č</b>	
<ul> <li>Last month you took the SAT/GRE and scored 750</li> </ul>	
out of a possible 800 on the quantitative part	
For kicks, you decide to take the test again	
different questions, but of the same	
difficulty	
<ul> <li>assume that there was no learning or</li> </ul>	
practice effect from the first test	
What score should you/we predict for you on the	
second test?	
<ul> <li>The surprising answer is that you are more likely to</li> </ul>	
score <b>below</b> 750 than <b>above</b> 750	
<ul> <li>the best guess is that you would score about 725</li> </ul>	
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### Regression to the Mean

Phenomenon discovered by Francis Galton, half cousin of Charles Darwin
Developed a regression analysis of height between human children and their parents

Found that "It appeared from these experiments that the offspring did not tend to resemble their parents in size, but always to be more mediocre than they - to be smaller than the parents, if the parents were large; to be larger than the parents, if the parents were small."

In fact, this applies only to extreme values

# A way to understand regression to the mean

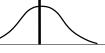
A given test is really a sample from a distribution. Assume that there is a large number, say 1,000 forms of a test and that

you take all 1,000 tests

• there are no learning, practice, or fatigue effects.

Scores will be distributed:

Identify the mean of this distribution as the "true score"



A way to understand regression to the mean - 2 Differences in the scores on these tests are due to <i>chance</i> factors: guessing knowing more of the answers on some tests than on others.	
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# A way to understand regression to the mean - 3

How could a first score of 750 have arisen:

- It reflected the true score (all chance factors balanced out)
- Your true score was <750 and you scored above it due to chance factors pushing you up
- Your true score was >750 and you only scored 750 due to chance factors dragging you down
- Which is more likely?
  - There are very few people with "true" scores above 750 (roughly 6 in 1,000)
  - There are many more people with true scores between 700 and 750 (roughly 17 in 1,000).
  - Thus, it is more likely that you are from the latter group

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# A way to understand regression to the mean - 4

Same principle applies to anyone at an edge of the normal distribution

More likely their true score is less different from the mean than the score obtained on a particular occasion when they obtained a very high score

- Baseball player who has a great or horrible batting average one year
- Sales representative who had a spectacular or horrible year

Why is it that most players who win "rookie of the year" honors perform less well their second year?

- A. By chance, the player performed above his/her natural level in the first year
- B. By chance, the player performed below his/her natural level in the second year
- C. Opposing players try harder against them
- The award winners don't try as hard the next year

# Regression to the mean and punishment

Makes it seem like punishment works: When someone is doing particularly poorly (for them), chastising them seems to result in better performance

But in fact it is only a case of regression

But praising someone does not seem to work: - When someone is doing particularly well (for them), praise is usually followed by poorer results

Just another instance of regression!

"Nature operates in such a way that we often feel punished for rewarding others and rewarded for punishing them" (David Myers, Intuition, p. 148).

Watch out for pseudo

### explanations

 A program proposes to help those who score at the very bottom end of a standardized test
 For example, intervenes with those scoring

less than 300 on the SAT

After the intervention, the individuals are tested again

 A larger proportion of this group exhibits improved scores than decreased scores

The program claims success BUT – It may have contributed nothing!

The results might totally be due to regression to the mean

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Fallacy of Prediction 3: Explaining expected streaks	
ТНТТТННТТТ	
3.1415926535 8979323846 2643383279 5028841971	
ТНТТТННТТТ НТТТТНТННН НННТТНТНТТ ТНННННТТТТ	
6939937510 5820974944 5923078164 0628620899	
8628034825 3421170679 НННННТНННТ ТННТТТННТТ	
25	

### Hot hand?

If someone just hit three shots in a row, is it a good idea to pass to them? What if they had missed three in a row? Philadelphia 76ers' game data from the 1980-81 season (using all shots from the field)—success on next shot

Three Straight Hits	.46
Two Straight Hits	.50
One Hit	.51
One Miss	.54
Two Straight Misses	.53
Three Straight Misses	.56

Source: Gilovich, Vallone, and Tversky (1985, Cognitive Psychology,2%able 1)

# Fallacy of Prediction 4: Neglecting base rates

In trying to make predictions, we very often ignore the most important variable for making a prediction

Frank was drawn at random from a group of thirty lawyers and seventy engineers. He spends most of his free time hanging around his country club. At the bar he often talks about his regrets at having tried to follow in his esteemed father's footsteps. The long hours he spent slaving in school could have been better spent learning to be less quarrelsome in his relationships with other people.

Is Frank a lawyer or an engineer?

What to base predictions on? Would you answer this one any differently?	
Frank was drawn at random from a group of thirty engineers and seventy lawyers. He spends most of his free time hanging around his country club. At the bar he often talks about his regrets at	
having tried to follow in his esteemed father's footsteps. The long hours he spent slaving in school could have been better spent learning to be less quarrelsome in his relationships with other people. Is Frank a lawyer or an engineer?	

In a city in which two cab companies, Blue and Green, operate, a taxicab was involved in a nighttime hit and run accident

- 85% of the cabs in the city are Green, 15% Blue
- A eyewitness identified the cab as Blue
- The Court tested the ability of the witness to identify cab colors under appropriate visibility conditions, and he/she made the correct identification 80% of the time
   What is the probability that the cab involved was Blue?
- What is the probability that the cab involved was Blu ≈80%

≈60% ≈60%

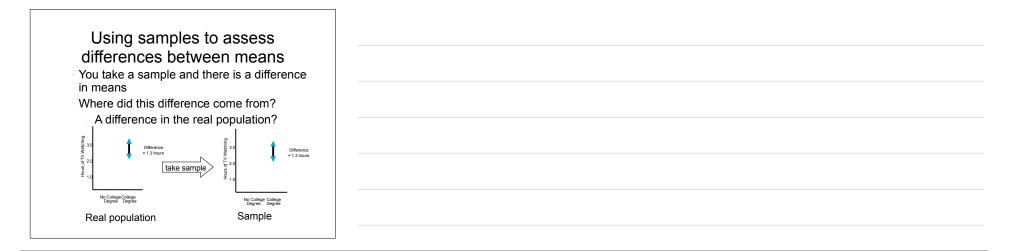
- ~00 % ≈40%
- D. ≈15%

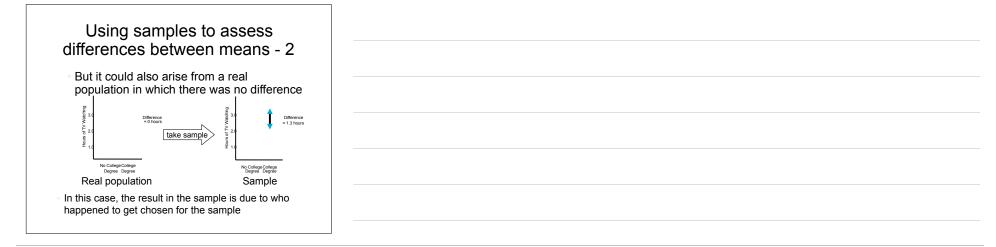
#### What to base legal decisions on? Said Blue Said Green Totals Blue 12 3 15 Green 17 68 85 Totals 29 71 100 Of the times he/she said it was Blue, it was blue 12/29 or 41% Is <50% accuracy good enough to convict?

Base Rates Base rates are often the best predictor It matters greatly whether the population was 70/30 lawyers or 70/30 engineers It matters greatly that 85% of the cabs were Green	
This trumps the witness's 80% accuracy!	
But humans almost universally ignore base rates if there is anything else on which to base the decision	
there is anything else on which to base the decision	
Police, lawyers, scientists, doctors	
- Even philosophy professors	

Comparing two populations	
<ul> <li>Populations defined in terms of nominal variables</li> <li>Men/women</li> <li>Gay/straight</li> </ul>	
Taking Phil 12/not taking Phil 12	
<ul> <li>Compare the two populations on another variable. If this variable is a score variable, ask:</li> <li>Do the distributions differ?</li> </ul>	
• Do the means differ?	
Do the variances differ? (asked much less often)	
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# How to tell whether a sample difference is real?

- What is the probability that the difference in the sample could have resulted by chance had there been no difference in the population?
- The hypothesis that there is no difference between the means of the two groups is known as the *null hypothesis*.
- Strategy: try to reject the null hypothesis Conclude that there is a difference in the real population when the sample you get would be very unlikely were the null hypothesis true

#### A null hypothesis

- A. Is the claim that there is a difference in the means in the two actual population
- B. Is the claim that there is no difference in the means in the two actual populations
- Is the claim that there is no difference in the means in the two samples
- Is the claim that the difference in means in the samples is the same as that between the actual populations

## Testing ESP



- Your friend claims to have extrasensory perception—ESP Being a good skeptic, you want to put
  - him to the test
- You use a set of five cards, each randomly presented twice
- You look at and think about the symbol on the card Your friend tries to figure out the symbol on the card
- you are looking at You do this ten times, and your friend gets
- 2 right
- 3 right
- 4 right
- 5 right
- How many does your friend have to get right before you are impressed?

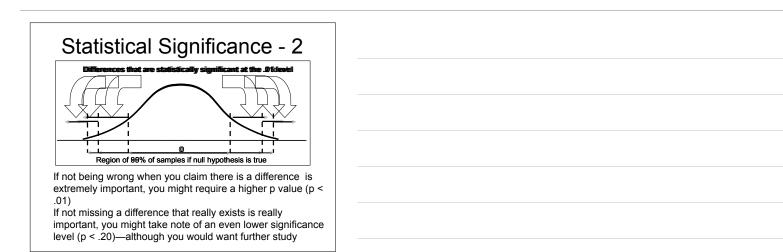
Two correct out of 10 trials is the most likely result if the null hypothesis were trueNumber of correct answersProbabilit yBut results of 0, 1, 2, 3, 4 are all quite likely even if the null hypothesis were true9.00000+How unlikely a result should we demand?6.00551How important is it to be right about ESP?3.201331268440.10737	Testing E	SP - 2	
null hypothesis were true10.000004But results of 0, 1, 2, 3, 4 are all quite likely even if the null hypothesis were true9.00000+How unlikely a result should we demand?6.00551How important is it to be right about ESP?3.201331.26844			
9         .00000+           But results of 0, 1, 2, 3, 4         8         .00007           are all quite likely even if the null hypothesis were true         6         .00551           How unlikely a result should we demand?         4         .08808           How important is it to be right about ESP?         2         .30199		10	.00000+
are all quite likely even if the null hypothesis were true       7       .00079         How unlikely a result should we demand?       6       .00551         How important is it to be right about ESP?       3       .20133         1       .26844	Indii Hypothesis were ti'de	9	.00000+
null hypothesis were true       1       100010         How unlikely a result should we demand?       6       .00551         How important is it to be right about ESP?       3       .20133         1       .26844		8	.00007
6     .00551       How unlikely a result should we demand?     5     .02642       How important is it to be right about ESP?     3     .20133       1     .26844		7	.00079
we demand? How important is it to be right about ESP? 4 .08808 3 .20133 2 .30199 1 .26844	null hypothesis were true	6	.00551
How important is it to be right about ESP?         3         .20133           1         .26844	How unlikely a result should	5	.02642
be right about ESP?	we demand?	→ 4	.08808
be right about ESP? 2.30199 1.26844	<ul> <li>How important is it to</li> </ul>	→ 3	.20133
		2	.30199
0 .10737	-	▶ 1	.26844
		• 0	.10737

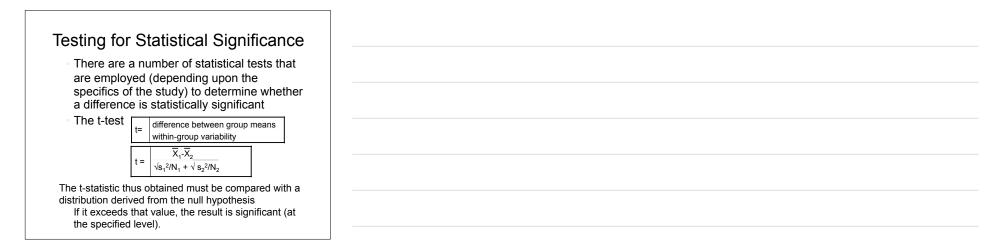
SP - 2	
Number of correct answers	Probabilit y
10	.00000+
9	.00000+
8	.00007
7	.00079
6	.00551
5	.02642
➡ 4	.08808
➡ 3	.20133
2	.30199
▶ 1	.26844
• 0	.10737
	<b>-</b>

Statistical significance again	
<ul> <li>Just as with correlations between score variables, we use the notion of statistical significance to evaluate results</li> </ul>	
<ul> <li>A difference in a sample is said to be <i>statistically significant</i> when it has a very low probability of occurring if the means in the population are equal</li> <li>How low a probability is very low?</li> <li>Investigators have to specify how high a probability they are willing to accept of being wrong</li> </ul>	
For many purposes, scientists accept a 1/20 risk of being wrong—5% (p < .05)	

If it is extremely important not to claim a difference between populations when there isn't one, one should

- A Insist that the difference in the means of the samples be large
- B. Not worry about p-values since they aren't important
- Insist on a p-value <.01 rather than <.05
- □. Insist on a p-value <.1 rather than <.05





# What has beer taught science?

William Sealey Gosset: So that future statistics s (who would surely com for his test) couldn't find published under the nar



Trained as a chemist brewery in Dublin

ked at the Guinness

How to determine, from small samples, which ingredients gave the best results?

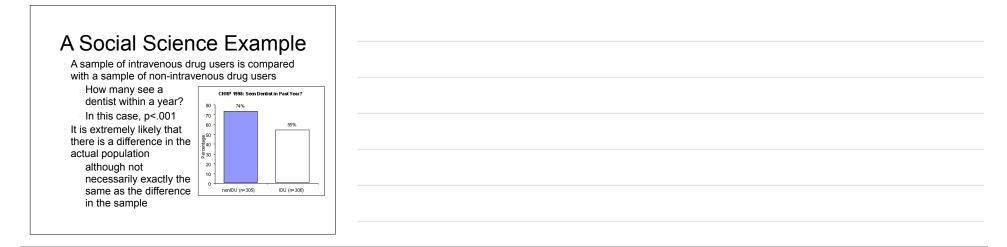
Published anonymously to avoid being accused of giving away trade secrets

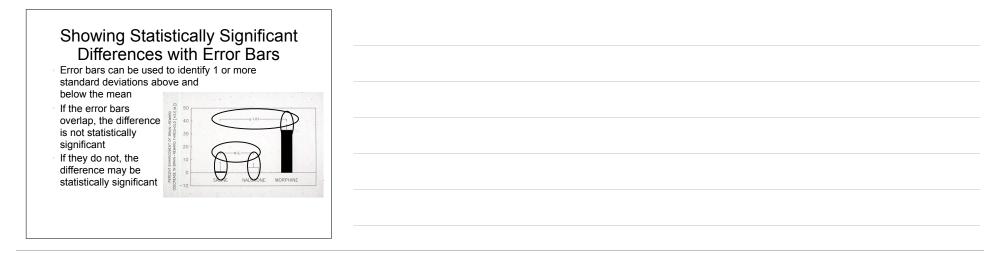
### A biological example

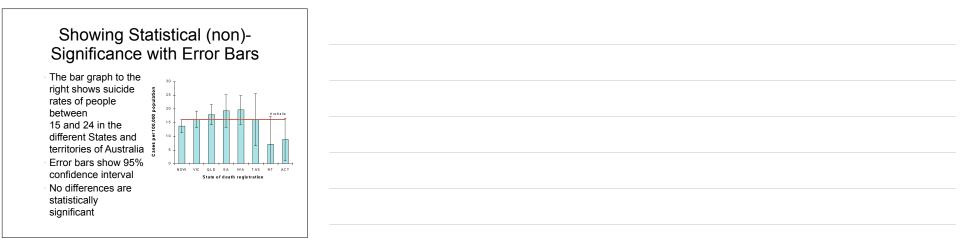
Biomass produced by two strains of bacteria

Bacterium A	Bacterium B
520	230
460	270
500	250
470	280

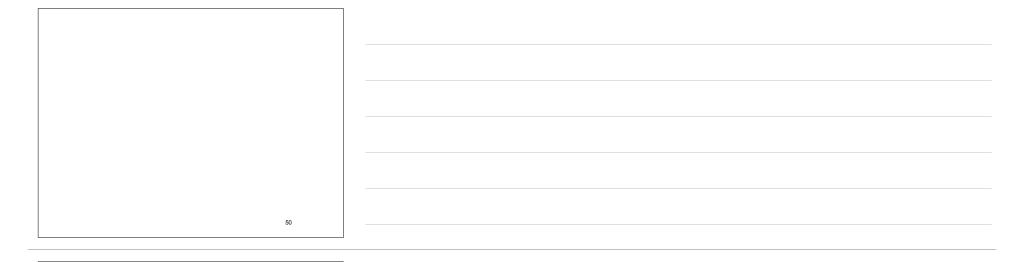
Are these differences reliable? t-statistic = 13.01 Criterion value for p<.05 is 2.45 Criterion value for p<.001 is 5.96 Result is significant at p<.001







Non-significant Difference versus	
No Difference	
If the difference in your sample is not significant, you conclude that you cannot tell whether there is	
actually a difference in the real population	
<ul> <li>There may be one, but the power of your test was too weak to find it</li> </ul>	
<ul> <li>It is important to keep in mind that we impose a high standard on significance</li> </ul>	
If we use p<.05, the result is not likely to happen more than 1 in 20 times by chance	
If p is only <.1, then the result is typically termed non-significant, but 9 times out of 10 there is a difference in the actual population	
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## Coincidences happen

Loarraine and Levinia Christmas are twins. They set out to deliver Christmas presents to each other near Flitcham, England. Their cars collide! Philip Dodgson, a clinical psychologist at South Downs heath center in Sussex, England, does psychotherapy with clergy and members of religious orders. He surfs the web to see if there are is anyone else named Philip Dodgson. He finds one in Ontario and writes to him.

The second Philip Dodgson is also a clinical psychologist working at Southdown Center, a residential psychotherapy center for clergy and members of religious orders!