# **Predicting Relations** between Variables

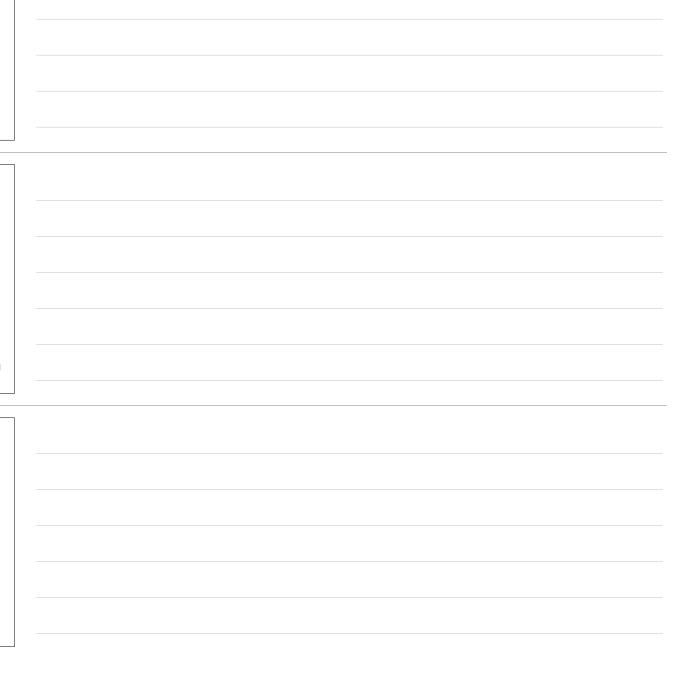
#### Where we have been

- . Hypotheses: conjectures about the way some phenomenon behaves
  - Need to be tested by predictions
  - Can be stated in terms of variables
- . Variables: things that vary
  - Variables differ in the way they can be measured
  - Nominal & ordinal vs score variables
- . Hypotheses about how a single variable is distributed
  - . Ages of people in food court
  - Amount of time animal spends foraging
  - Amount of time you spend studying

#### Hypotheses involving more than one variable

Many of the hypotheses of interest in science and in ordinary life involve relations between variables

- Amount of sleep and ability to recall information
- Pressure, volume, and temperature of a gas
- Experience and job performance
- SAT score and grades in college
- Vitamin intake and health condition
- Sexual activity and sexually transmitted
- diseases
- Smoking and lung cancer
- Miles per gallon and horsepower of cars



## The Case Against Bread

- More than 98% of convicted felons are bread
- Fully half of all children who grow up in bread consuming households score below average on standardized tests.
- In the 18th century, when virtually all bread was baked in the home, the average life expectancy was less than 50 years.



- More than 90% of all violent crimes are committed within 24 hours of eating bread.
- Primitive tribal societies that have no bread exhibit a low incidence of cancer, Alzheimer's, and Parkinson's disease.
- · Ask yourself: are the statistics meaningful!

# Correlational and causal hypotheses

- Many of the hypotheses of interest in science and in ordinary life are causal
  - Red wine and (reduced) cholesterol levels
  - Smoking and lung cancer
  - Vitamin C and prevention of colds
  - Tax cuts and economic recovery
  - Use of imagery and increased memory
- But causal claims are more difficult to establish than correlational claims
  - . So for now we focus on correlations only

# **Correlations and why they** are interesting

- . A correlational claim is a claim that the values on two variables vary systematically
  - Not necessarily in the same direction
- . Why care about correlations if they are not (known to be) causal?
  - They may indicate causal relations
  - They can be used to make predictions about the unknown value of one variable from the known value of another variable



# SAT and College Grades

- Should the SAT be used as a (or maybe the) basis for admission to the University of California?
- If so, then it must be justified
  - Does it predict success in college?
  - If it doesn't, then it may be an inappropriate measure to use in judging admissions
- Compare: basing admissions to UC on
  - Running speed for the mile
  - · Length of one's index finger

#### **Clicker Question**

For shoe size to be used as a basis for deciding on life insurance rates

Shoe size must be a score variable

There must be a high percentage of those with large shoe sizes among those who live long

An individual's shoe size must be a good predictor of life expectancy

Shoe size could never be employed as a basis for deciding on life insurance rates

# Correlational Research Examples

- Is there a relationship between family income and grade point average?
- Is there a relationship between number of hours of part time employment and grade point average?
- Is there a relationship between years of education and income later in life?

# From the general to the testable

- Not all hypotheses relating variables are directly testable—hypotheses presented in general terms
  - Force is equal to mass x acceleration
  - Fitter people live longer
  - Better education correlates with greater happiness
  - Greater pollution correlates with greater global warming
  - Animals living in colder climates are larger
  - Former players of contact sports suffer more brain damage

# **Testable predictions**

- To test hypotheses such as these, we need to make specific predictions
  - Predictions which can be evaluated
  - Must predict something that we can detect and measure, either with our senses directly or via instruments

# **Operational "definitions"**

- Relate the variables used in the hypothesis to measurable variables
- Variables such as force, memory ability, happiness, brain injury, etc., are not directly measurable (observable).
  - Must specify a measurement procedure and a variable we can measure
- The operational definitions of any nonobservational terms are major auxiliary assumptions in any test of a hypothesis

#### **Distance**

• Inch: width of a grown man's thumb



- King Edward II (14th C.): the length of an inch shall be equal to three grains of barley, dry and round, placed end to end lengthwise
- Foot: the name gives away its original reference
   Standardized to 12 inches
- Yard: the length of a person's belt
  - King Henry I (13th C.): distance from his nose to the thumb of his outstretched arm, which was about 36 inches



# The meter standard



- The meter introduced by the French in 1791 as one ten millionth of the distance from the equator to the north pole along a meridian through Paris
  - Standard meter bar: A platinum bar with a rectangular cross section and polished parallel ends at a specific temperature
- 1859: J.C. Maxwell defined it in terms of the wavelength of the yellow spectral line of sodium
- 1892: A.A. Michelson 1,553,164.13 times the wavelength of cadmium red in air, at 760 mm of atmospheric pressure at 15° C.

## The standard meter - 2



1960: 1,650,763.73 vacuum wavelengths of light resulting from orange-red light, in a vacuum, produced by burning the element krypton (Kr-86).



1983: length of the path traveled by light in vacuum during 1/299,792,458 of a second

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#### The case of IQ

 In 1904 Alfred Binet was commissioned by the French government to devise a test to differentiate children who would not do well in usual schools from those who would

The latter were to be assigned to special schools with greater individual attention but where they would not disrupt the intellectually normal children

"It seems to us that in intelligence there is a fundamental faculty, the alteration or the lack of which, is of the utmost importance for practical life. This faculty is judgment, otherwise called good sense, practical sense, initiative, the faculty of adapting one's self to circumstances. A person may be a moron or an imbecile if he is lacking in judgment; but with good judgment he can never be either. Indeed the rest of the intellectual faculties seem of little importance in comparison with judgment" (Binet & Simon, 1916, 1973, pp.42-43).

## The case of IQ - 2

 30 item test, with different questions typically solved by children at different ages

One of these is a square and one is not. which one is the square?



attend to simple instructions

- name parts of the body
- compare lengths and weights
- count coins
- · assess which of several faces is "prettier"
- name objects in a picture
- · remember digits from a list
- define words
- · fill in the missing words in sentences

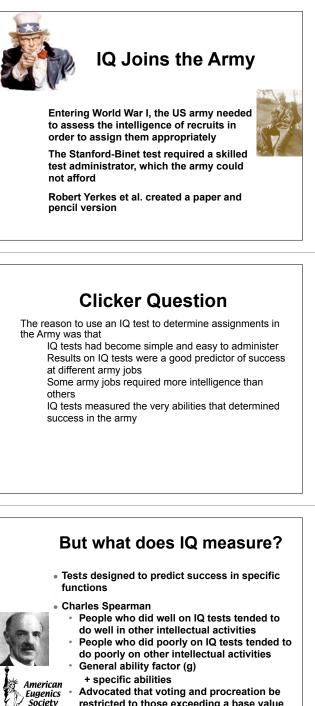


## The case of IQ - 3

- Intelligence Quotient (William Stern—1914):
   age level of test results/chronological age, normed to 100
  - an 8 year old who passes the 10 year-old's test would have an IQ of 10/8 x 100
- Lewis Terman of Stanford (1916):
- Items on Binet's test didn't predict well in California so revised the test—Stanford-Binet
- Extended test to adults: instead of ratios, employed standard deviations (1 SD= 15 pts)
- Introduced "IQ"
- Studied, and *promoted*, 1000+ of those who scored high
- · Advocated forced sterilization of "feebleminded"



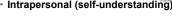
restricted to those exceeding a base value for g

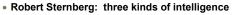


# **Beyond IQ?**



- Verbal
- Mathematical
- Musical
- Spatial
- Kinaesthetic
- Interpersonal (social skills)
- Intrapersonal (self-understanding)







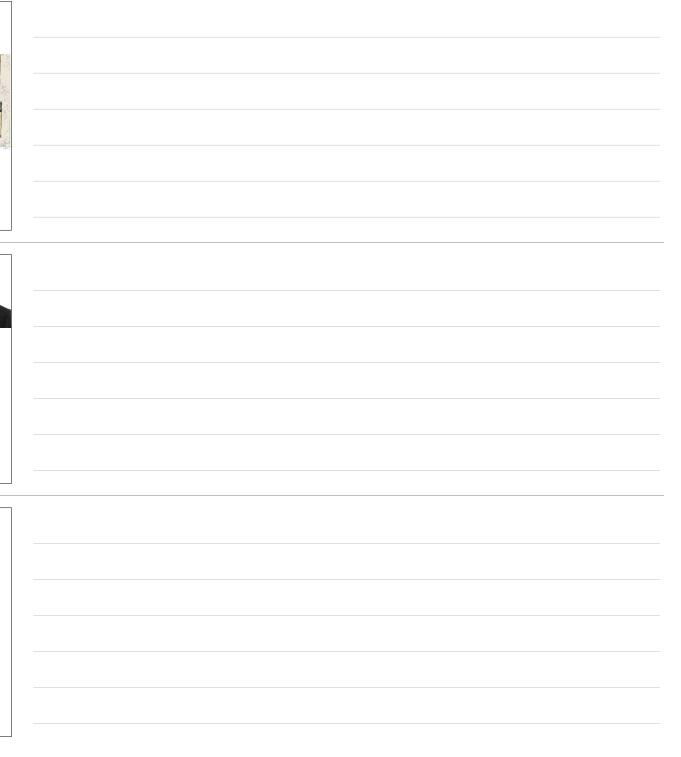


• In the early 1980s James Flynn, a New Zealand political scientist, discovered that the IQ in various groups of people increased on average 3 points per 10 years.

- Effect replicated throughout the industrialized world
- Hidden by the fact that IQ tests are regularly renormed to keep the mean at
- Increases apparently not linked to learning— greatest increases in non-verbal tests of intelligence
- Explanation ? ? ?

# **Construct Validity**

- Does the way you operationalize a variable really measure that variable?
  - Does a ruler (do grains of barley) really measure height?
  - Does an intelligence test measure intelligence?
  - Does a word-list test measure memory?
- The degree to which a measure measures what it is supposed to measure is referred to as its construct validity



# **Clicker Question** An operational definition Aims to provide necessary and sufficient conditions for the variable being being measured Employs operations to determine what something is Relates a variable used in a hypothesis to a way to measure it Provides sufficient, but not necessary conditions for the variable being measured **Clicker Question** Construct validity is concerned with Whether the argument for the construct is valid Whether the operational definition really measures the variable used in the hypothesis Is only important if there is doubt about how to assign values to variables Replacing operational definitions with real definitions **Operational definitions are** not definitions

An operational definition provides one way to measure a variable

There will typically be alternatives
The alternatives may not always agree

Even when construct validity is high, the operational definition does not provide necessary and sufficient conditions for the term

# **Relating Score Variables**

- Same items measured on two score variables
- Is there any systematic relation between the score on one variable and the score on another?

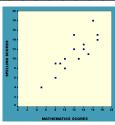
Participant	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Spelling	15	14	15	12	6	4	8	9	9	12	18	13	10	10	11
Math	12	17	17	12	8	5	10	9	8	14	16	14	10	13	15

Often it is difficult to determine if there is a regular pattern by just looking at scores (eyeballing the data)

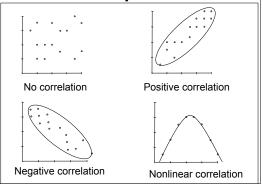
Important to graph or diagram the data

# **Scatterplots**

ĺ	Participant	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	Spelling	15	14	15	12	6	4	8	9	9	12	18	13	10	10	11
	Math	12	17	17	12	8	5	10	9	8	14	16	14	10	13	15



# Scatterplots - 2



# **Measuring correlation**

Karl Pearson developed a measure of correlation, known as Pearson's Product Moment Correlation (r)

A Z score for an individual is how many standard deviations that individual is from the mean. From that there is an easy calculation of Pearson's r:

$$r = \sum (ZxZy) / N$$

$$r = \frac{\Sigma XY - \frac{\Sigma X \Sigma Y}{N}}{\sqrt{(\Sigma X^2 - \frac{(\Sigma X)^2}{N}) - (\Sigma Y^2 - \frac{(\Sigma Y)^2}{N})}}$$

# Pearson Correlation Coefficient

Participant	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Spelling	15	14	15	12	6	4	8	9	9	12	18	13	10	10	11
Math	12	17	17	12	8	5	10	9	8	14	16	14	10	13	15

- Pearson's Product Moment Correlation r = .857
  - Note: Positive Value—positively correlated
  - Value close to 1—strongly or highly correlated
- Strong positive correlation

## **Clicker Question**

A Pearson correlation of 4.25 between height and salary Represents a very strong positive correlation Means that height is a very good predictor of salary Means that height is a poor predictor of salary Makes no sense

# **Clicker Question**

A study correlating age and interest in health care resulted in a correlation -0.37. This indicates

Increased age is a very strong predictor of greater interest in health care

Increased age is a moderate predictor of greater interest in health care

Increased age is a moderate predictor of lesser interest in health care

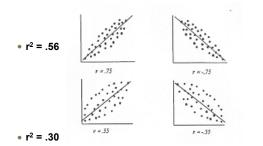
There is no basis for predicting interest in health

# How much does the correlation account for?

- Correlations are typically not perfect (r=1 or r=-1)
  - Evaluate the correlation in terms of how much of the variance in one variable is accounted for by the variance in another [variance=∑ (X-mean)²/N]
- [variance=∑ (X-mean)²/N]

   Amount of variance accounted for (on the variable whose value is being predicted) equals:
- Variance explained/total variance
   This turns out to be the square of the Pearson
- coefficient: r<sup>2</sup>
   So:
  - if r=.80, then we can say that 64% of the variance is explained.
  - If r=.30, then we can say that 9% of the variance is explained.

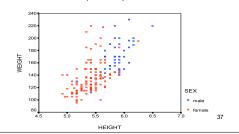
## **Variance Accounted for**



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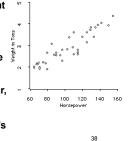
#### Variance accounted for - 2

Height only partially accounts for weight
 For females, r = .47, so r<sup>2</sup>=.22
 For males, r = .68, so r<sup>2</sup>=.46



## Variance accounted for - 3

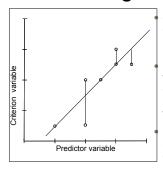
- Correlating automobile horsepower and weight
   r = .92
- r = .92
   r<sup>2</sup> = .81
- Horsepower accounts for 81% of the variance in car weight
  - Given only the horsepower of a car, you can make a quite reliable estimate of the car's weight



## **Prediction**

- A major reason to be interested in correlation
  - If two variables are correlated, we can use the value of an item on one variable to predict the value on another
    - Employment prediction: future job performance based on years of experience
    - Actuarial prediction: how long one will live based on how often one skydives
    - Risk assessment: prediction of how much risk an activity poses in terms of its values on other variables
- Prediction employs the regression line

# **Regression line**



Start with scatter plot of data points

Find line which allows for the best prediction of the criterion variable (one to be predicted) from that of the predictor variable

Line which minimizes the (square of the) distances of the blue lines

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# **Regression line**

- y = a + bx
- y = predicted or criterion variable
- x = predictor variable
- a = y-intercept—regression constant
- b = slope—regression coefficient
- Note: the regression coefficient is not the same as the Pearson coefficient r

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## **Clicker Question**

If the Pearson coefficient (r) between age and liking for chocolate is -.62, what can you infer about the slope of the regression line?

- Nothing
- B. The slope is also -.62
- C. The slope will be .62
- D. The slope will be negative

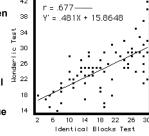
# Understanding the Regression Line

- Assume the regression line equation between the variables mpg (y) and weight (x) of several car models is
  - mpg 62.85 0.011 weight
  - MPG is expected to decrease by 1.1 mpg for every additional 100 lb. In car weight
  - The regression constant 62.85, represents the projected value of a car weighing 0 lbs.

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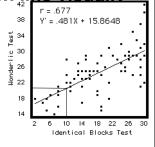
- Correlation between
- Identical Blocks
   Test (a measure of spatial ability)
- Wonderlic Test (a measure of general intelligence)
- Calculate new value for x = 10:
- y = .48 x 10 + 15.86 = 20.67



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# Interpolating from the regression line visually

- Draw line from the x-axis to the regression line
- Draw line from the intersection with the regression line to the y-axis



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# Clicker Question You are told that the regression line relating a reasoning test score and a memory test score is reasoning score = -3.25 + .7 memory score You know that A. There is a positive correlation between the scores B. There is a negative correlation between the scores C. Pearson's r = .7 D. Pearson's r = -3.25